



Designing a Low- Pass FIR Digital Filter by using Rectangular Window Hanning Window and Bartlett Method

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Abstract: Digital filtering plays a significant role in the world of technology. Therefore, processing of input signal has to be done to get useful signal. This paper deals with the design of finite impulse response digital filter using window techniques Rectangular, Hanning and Bartlett of order (15) are presented. It shown that filterdesign by using Rectangular Window Technique is better as it provides better result in terms of magnitude, phase, impulse, step responses and pole-zero plot.[1]

Keywords: FIR Filter, DSP, FFT, Hanning Window, MATLAB, Rectangular Window, Bartlett Window, frequency sampling, amplitude-frequency.

1. INTRODUCTION

Digital signal processing is the technique employed for the mathematical manipulation of an information signal so as to modify or improve it. For this purpose filters are mainly used[2]. The filter is used to describe a linear time-invariant system used to perform spectral shaping or frequency selective filtering. Filter is used in digital signal processing is widely used a number of ways, such as equalization of communication channels, signal detection in radar, sonar and communications, and for performing analysis of the spectra of a variety of signal [3]. A digital filter is a system which passes some desired signals more than others to reduce or enhance certain aspects of that signal. It can be used to pass the signals according to the specified frequency pass-band and reject the other frequency than the pass-band specification [4]

Application of digital signal processing

Military – radar signal processing, sonar signal processing, navigation, secure missile guidance.

Image processing – image representation, image compression, image enhancement, satellite weather map and animation, robotic vision, image analysis recognition

Medicine- Medical diagnostic instrumentation such as computerized tomography (CT), X-ray scanning, Patient monitoring and Xray

Signal filtering- Removing of unwanted background noise, removal of interference, separation of frequency bands and shaping of the signal spectrum.

Telecommunication - Echo cancellation in telephone networks, equalization, telephone dialing application, modems, line repeaters, channel multiplexing, data encryption, video conferencing, cellular phone and FAX [5]

2. WINDOW TEECHNIQUE

The FIR filter design process using window function can be enumerated as:

- i. Define filter specification
- ii. Specify a window function according to the filterspecification.
- iii. Compute the filter order required for a given setof specification.
- iv. Compute the coefficients of the window functio to be used.
- v. Compute the coefficients the ideal filteraccording to the filter order.
- vi. Compute FIR filter coefficients in accordance the obtained window function and the coefficients ofthe ideal filter.
- vii. If the resulting filter has a very wide or a verynarrow transition region, it is mandatory tochange the filter order by decreasing it accordingto needs, and after this process the steps 4, 5 and6 are interated as many times as needs.



The window used in this paper to design the FIR filter are:

1. Rectangular window.
2. Hanning
3. Barlett [6]

2.1. RECTANGULAR WINDOW

The rectangular window is what you would obtain if you were to simply segment a finite portion of the impulse response without any shaping in the time domain:

$$w[n] = \begin{cases} 1, & 0 \leq n \leq M-1 \\ 0, & \text{otherwise} \end{cases}$$

We have studied this function extensively in class, and know it's DTFT to be $\omega(ej\omega) = \sin(M\omega/2) \sin(\omega/2) e^{-j\omega M/2}$

Compare the plots of the original sinc function above (without the phase term) and its magnitude plotted in dB, $20 \log_{10}(|\omega(ej\omega)|)$. [7]

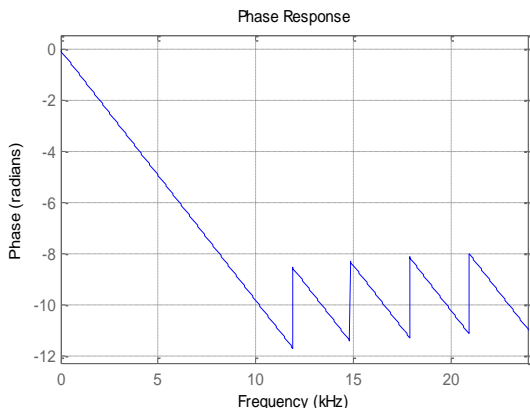


Fig.(1) Phase Respoce of Recantugar window

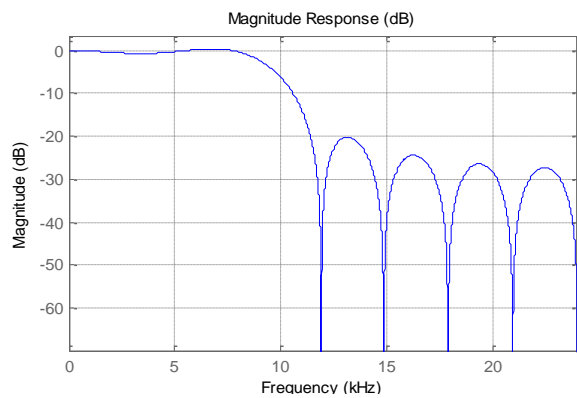


Fig.(2) Magnitude Response of Recantugar window

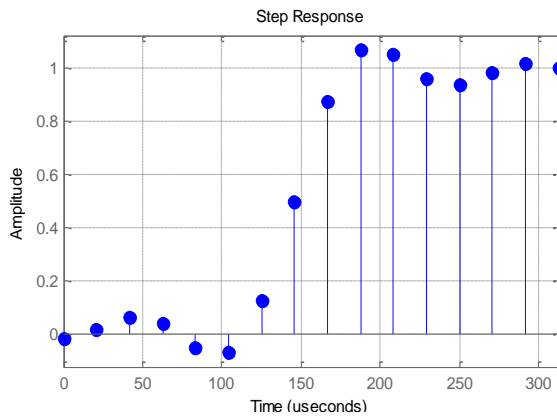


Fig.(3) Step Response of Rectangular window

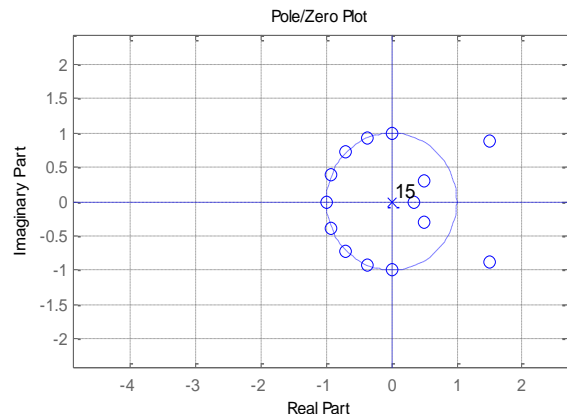


Fig.(4) Pole/Zero Plot of Rectangular window

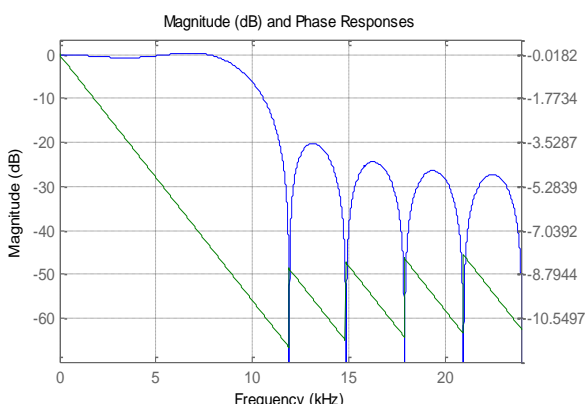


Fig.(5) Magnitude and Phase Responses of Rectangular

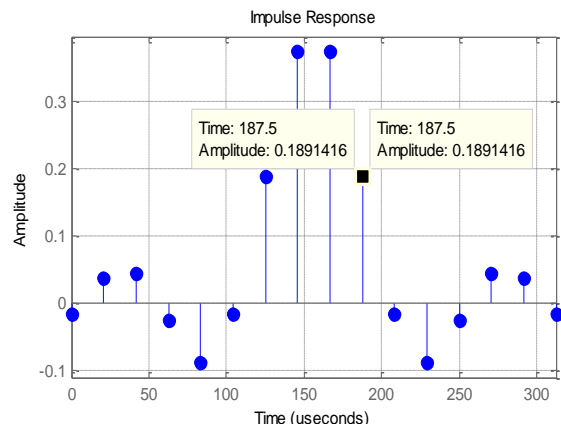


Fig.(6) Impulse Response of Rectangular Window



```

Numerator:
-0.015669003171969013
 0.037481440133332426
 0.044296247430301965
-0.026115005286615065
-0.086988830699091871
-0.016033215553239631
 0.18914159983317316
 0.37388676731410792
 0.37388676731410792
 0.18914159983317316
-0.016033215553239631
-0.086988830699091871
-0.026115005286615065
 0.044296247430301965
 0.037481440133332426
-0.015669003171969013
    
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Fig.(7) Coficcient of Rectangular window Technique

2.2Hanning window

Syntax: w = hann(L)

Description: It returns an L-point symmetric Hann window in the column vector w. L must be a positive integer.

The coefficients of a Hann window are computed from the following equation.

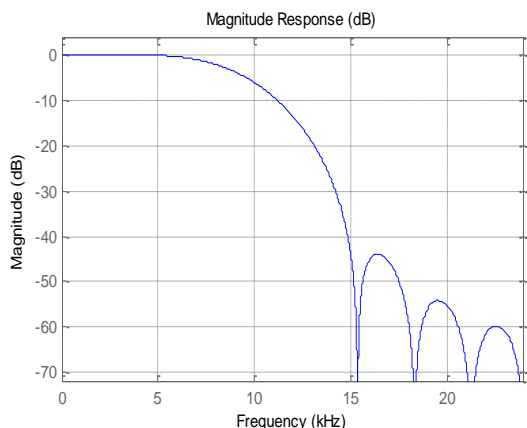


Fig.(8) Magnitude Response of Hanning window

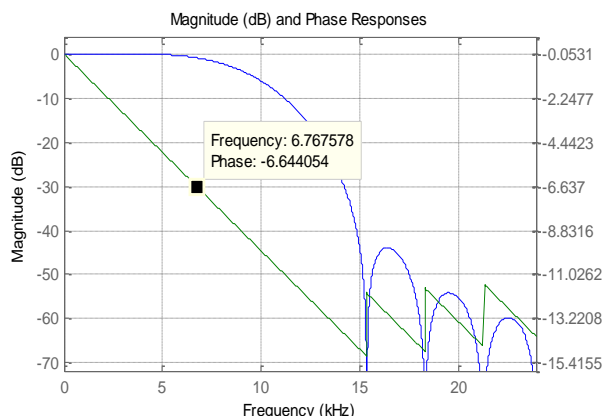


Fig.(9) Mangnitude and Phase Response of Hanning window

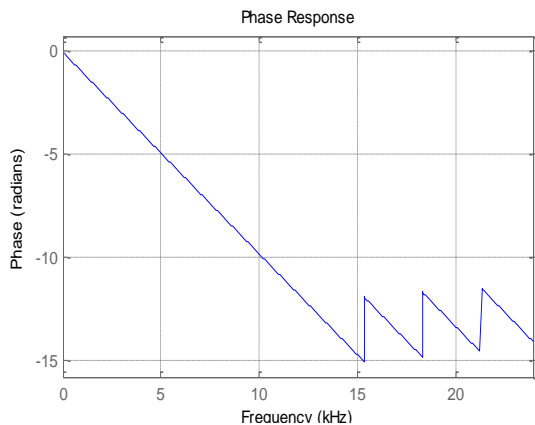


Fig.(10) Phase Response of Hanning window

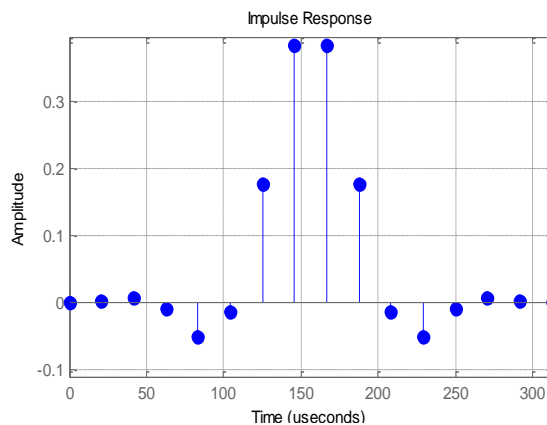


Fig.(11) Impulse Response of Hanning window

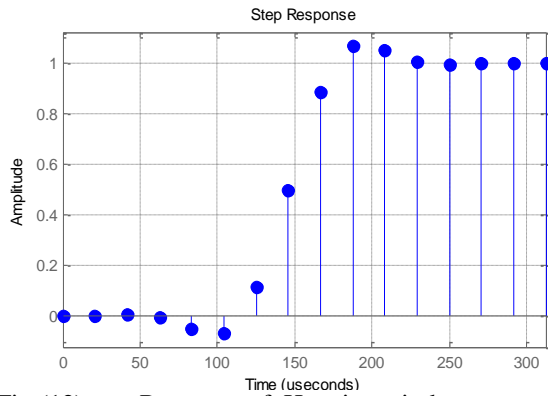


Fig.(12) step Response of Hanning window

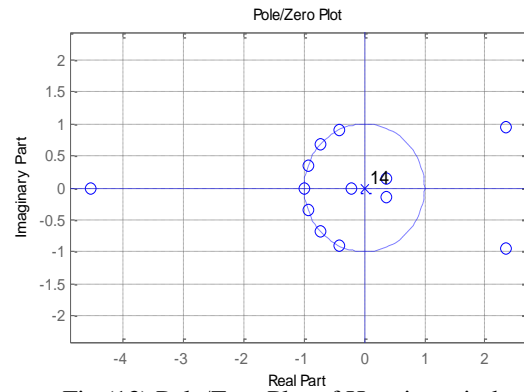


Fig.(13) Pole/Zero Plot of Hanning window

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Numerator:
0
0.0016851249777687343
0.0076216949469096081
-0.0093839463216623155
-0.049965292664107021
-0.012506619032844082
0.17793350568700897
0.38461553240692614
0.38461553240692614
0.17793350568700897
-0.012506619032844082
-0.049965292664107021
-0.0093839463216623155
0.0076216949469096081
0.0016851249777687343
0
    
```

FIG.(14) Filter Coefficient of Hanning window

2.3 The Bartlett window

The Bartlett window is very similar to a triangular window as returned by the triang function. The Bartlett window always has zeros at the first and last samples, however, while the triangular window is nonzero at those points. For L odd, the center L - 2 points of bartlett(L) are equivalent to triang(L-2).

w = bartlett(L) returns an L-point Bartlett window in the column vector w, where L must be a positive integer. The coefficients of a Bartlett window are computed as follows:

$$w_n = \begin{cases} \frac{2n}{N}, & 0 \leq n < \frac{N}{2} \\ \frac{2(N-n)}{N}, & \frac{N}{2} \leq n < N \end{cases}$$

8>>>>:

The window length L=N+1.

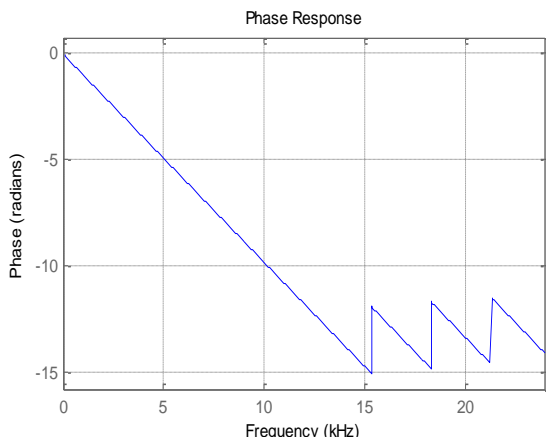


Fig.(15) Phase Response of Bartlett window

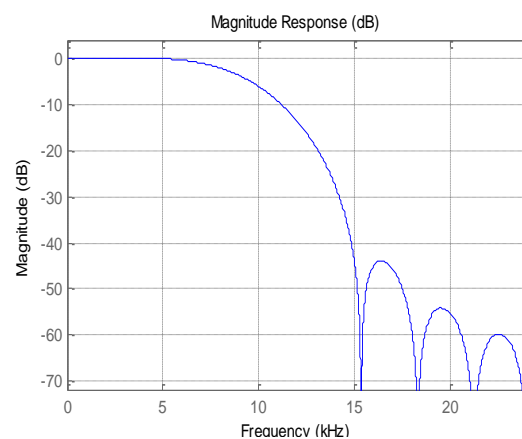


Fig.(16) Magnitude Response of Bartlett Window

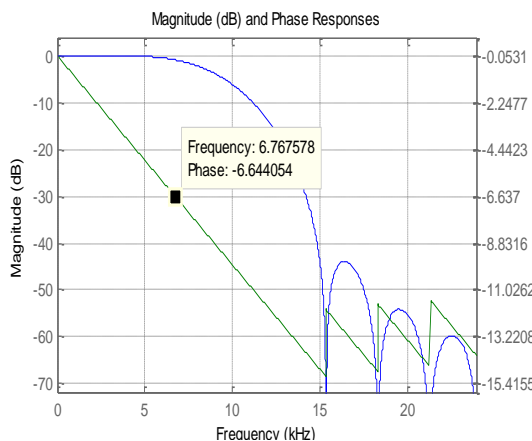


Fig.(17) Magnitude and Phase Response of Bartlett

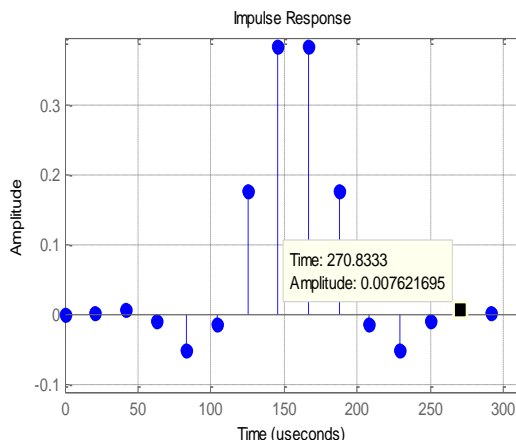


Fig.(18) Impulse Response of Bartlett window

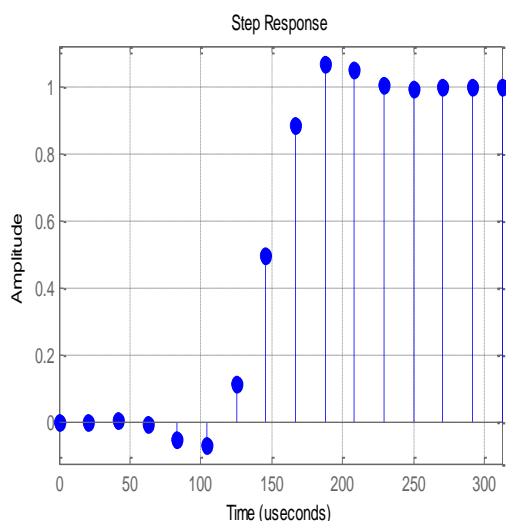


Fig.(19) Step Response of Bartlett window

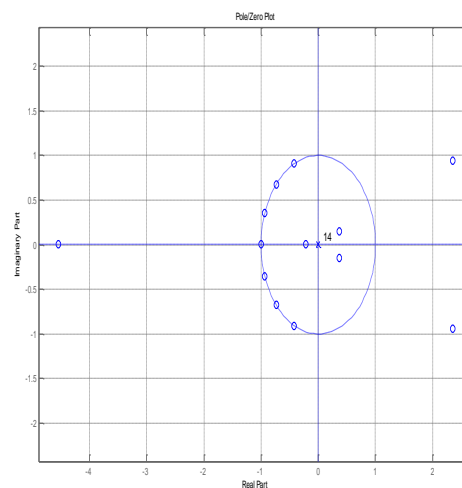


Fig.(20) Pole/Zero of Bartlett window

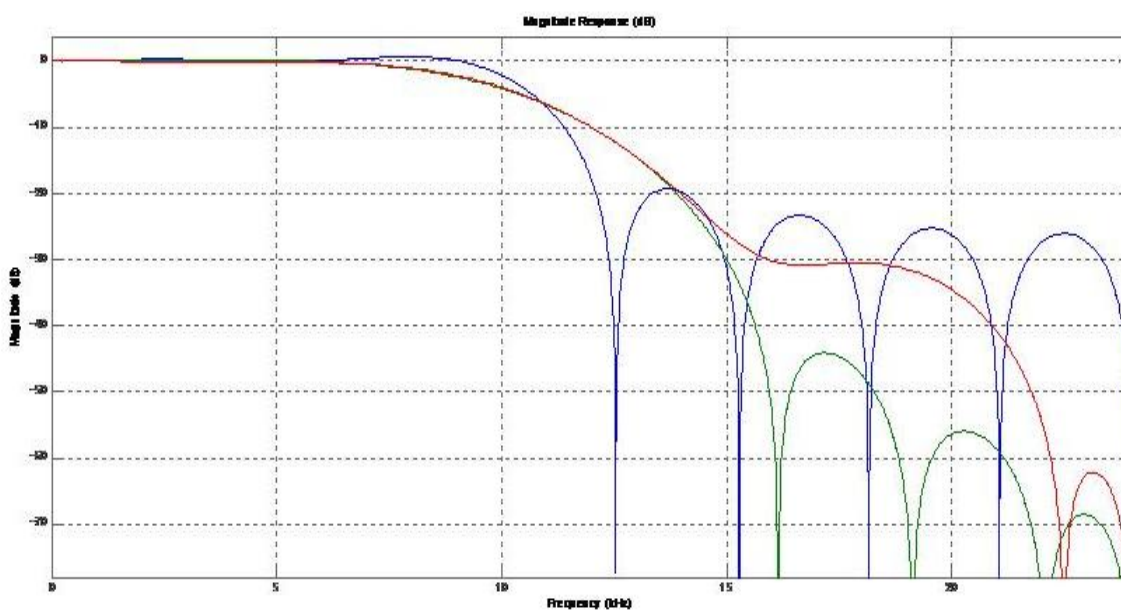


Fig.(21) Comparison of Magnitude Response of Rectangular Hanning and Bartlett window Technique

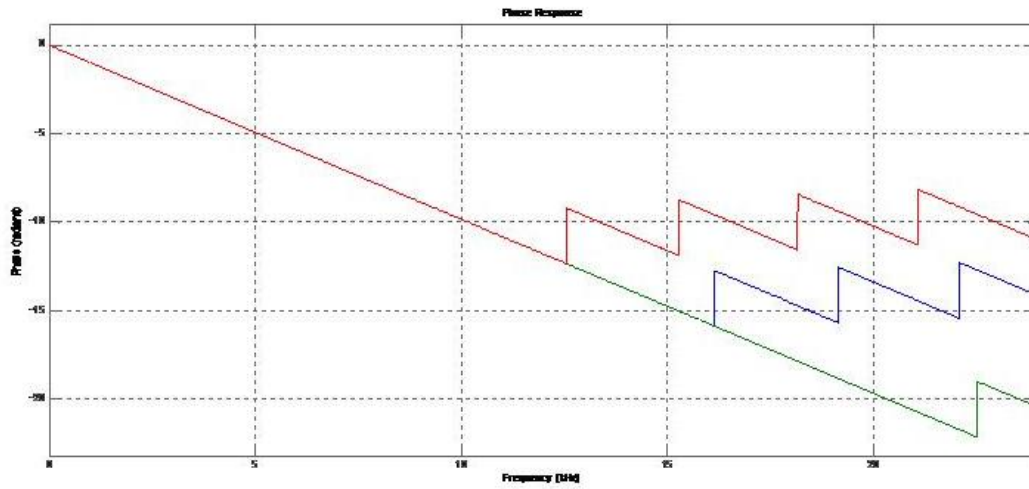


Fig.(22) Comparison of Phase Response of Rectangular Hanning and Bartlett Method

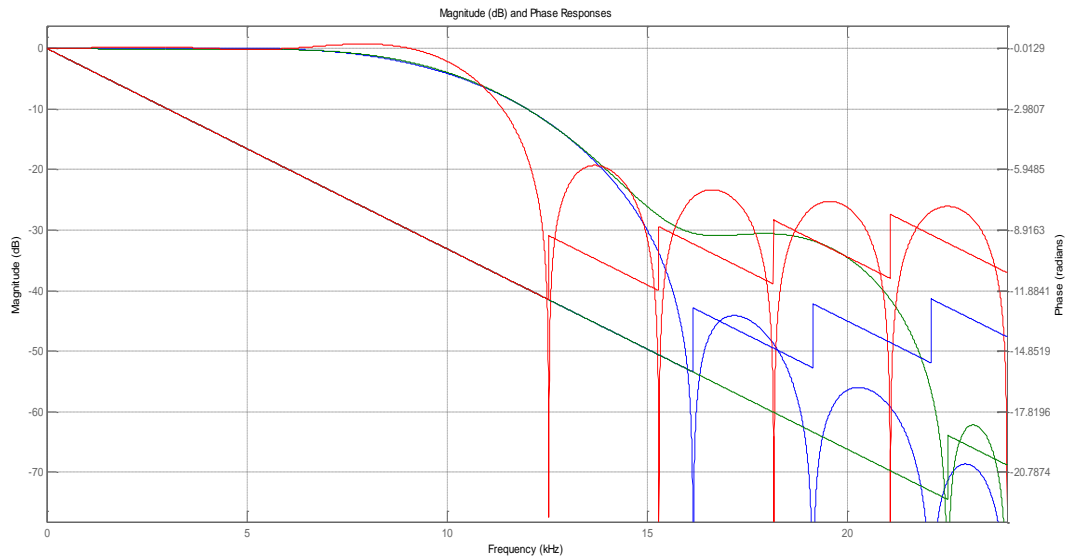
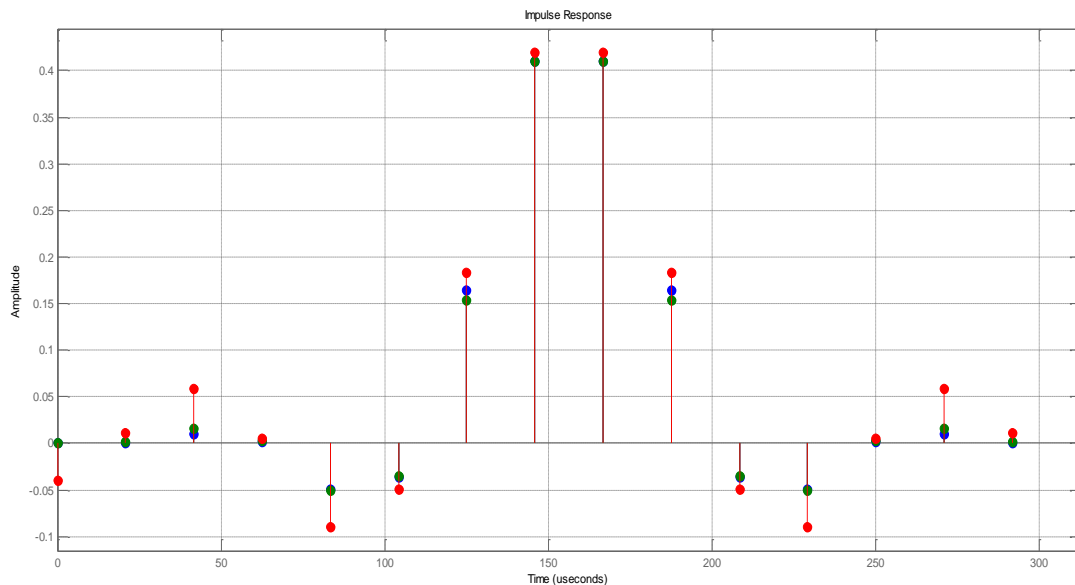


Fig.(24) Comparison of Magnitude and Phase Response of Rectangular Hanning and Bartlett Method



Fig(23) Comparison of Impulse Response of Rectangular Hanning and Bartlett Method

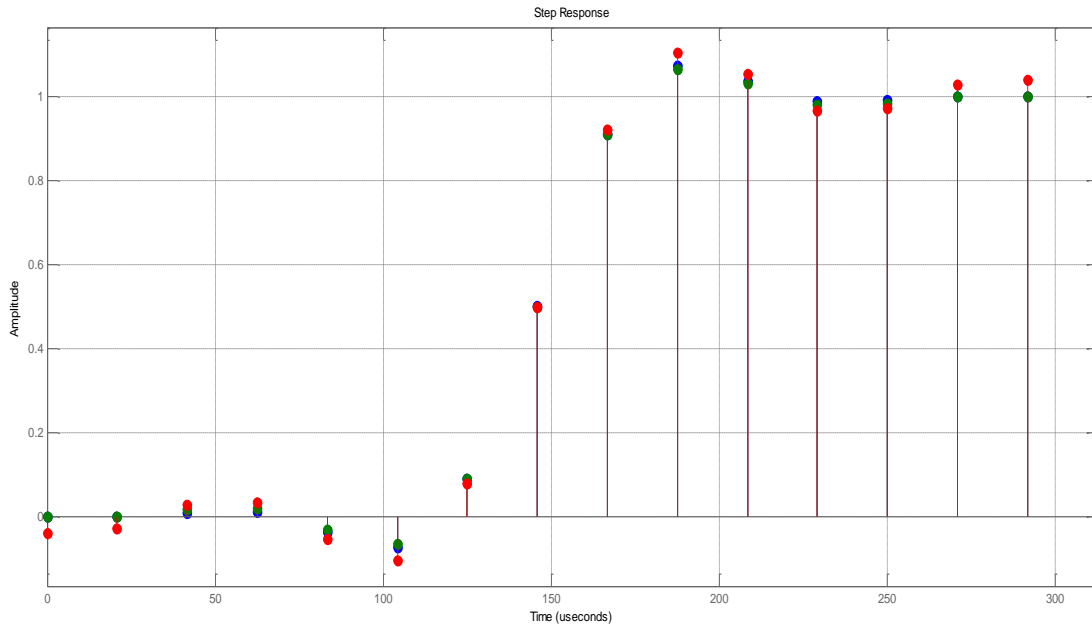


Fig.(24) Comparison of Step Response of Rectangular Hanning and Bartlett Method

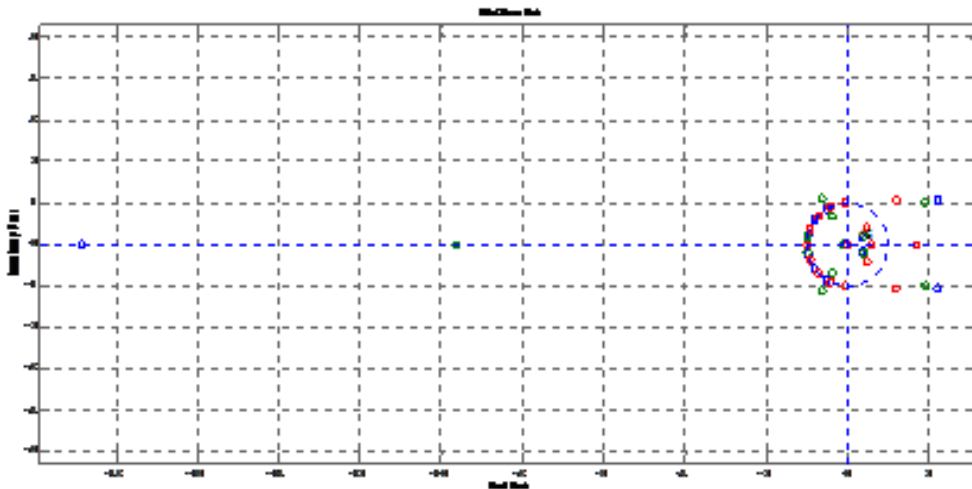


Fig.(25) Comparison of Pole/Zero Plot of Rectangular Hanning and Bartlett

3. RESULT

Simulation Result of MATLAB

Window Technique	Relative side lobe attenuation	Main lobe width (-3dB) Frequency	Leakage Factor
RECTANGULAR	-31.5	0.20313	0.05%
HANNING	-31.5	0.20313	0.05%
Bartlett	-25.3	0.17939	0.42%

4 CONCLUSIONS

In this paper FIR low pass filter has been designed and simulated using Rectangular, Hanning and Kaiser Window technique has been compared, In Signal processing applications digital filters are more preferable than analog filters. The digital filters are easily designed and also easy to use in various types of signal filtering applications. The choice of technique to design the filter depends on the decision of designer whether r to compromise accuracy of approximation or ease of design.



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BIOGRAPHIES



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